

**2017-yil matematika variant yechimlari (spectrum)**

**24-variant**

**Bizning kanal : @axborotnoma**

**Adminsratorlar hayati : @axborotnoma\_bot**

**Matematika yordam guruhi : @axborotnomaguruhi**

**Reklama xizmati : @axborotnoma\_reklama**

**24-variant**

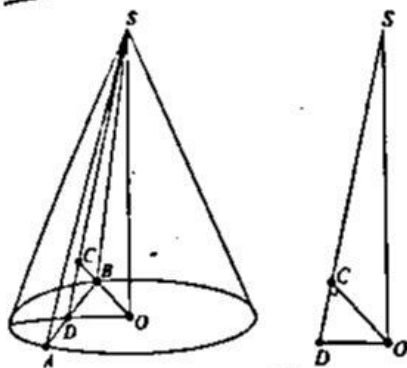
1. Konus asosining markazidan 3 sm masofada AB vatar o'tkazilgan. SO konus balandligi.  $SO = 6\sqrt{2}$  bo'lsa, O nuqtadan ASB tekislikkacha bo'lgan masofani toping.

**Yechish:**

$$OD = 3, SO = 6\sqrt{2}$$

$$SD^2 = SO^2 + OD^2 = (6\sqrt{2})^2 + 3^2 = 81$$

$$SD = 9$$



$$OC = \frac{SO \cdot OD}{SD} = \frac{6\sqrt{2} \cdot 3}{9} = 2\sqrt{2}$$

$$OC = 2\sqrt{2}.$$

Javob:  $2\sqrt{2}$ .

2.  $t^2 + t - 1 = 0$  bo'lsa,  $\left(t - \frac{1}{t}\right)^2$  ning

qiymatini toping.

**Yechish:**

$t^2 + t - 1 = 0$  bo'lsa  $\left(t - \frac{1}{t}\right)^2$  ning qiymatini

topamiz:

$$t^2 + t = 1 \quad | :t$$

$$\frac{t^2 + t}{t} = \frac{1}{t} \Rightarrow t + 1 = \frac{1}{t}$$

$$\left(t - \frac{1}{t}\right)^2 = (t - (t + 1))^2 = (t - t - 1)^2 = 1.$$

Javob: 1.

3.  $f(x) = 4 + 3\sin x$  funksiyaning  $(\pi; \pi)$  nuqtadan o'tuvchi boshlang'ich funksiyasini toping.

**Yechish:**

$$f(x) = 4 + 3\sin x, A(\pi; \pi),$$

$$F(x) = ?$$

1)  $f(x) = 4 + 3\sin x$  funksiyaning boshlang'ich funksiyasi.

$$F(x) = 4x - 3\cos x + C$$

$$2) (\pi; \pi), \pi = 4\pi - 3\cos\pi + C$$

$$C = -3\pi - 3.$$

$$3) F(x) = 4x - 3\cos x - 3\pi - 3 = 4x - 3(\cos x + \pi + 1).$$

Javob:  $4x - 3(\cos x + \pi + 1)$ .

4.  $\text{tg}20^\circ + \text{tg}40^\circ + \text{tg}60^\circ + \dots + \text{tg}160^\circ + \text{tg}180^\circ$  yig'indisini hisoblang.

**Yechish:**

1) keltirish formulasidan foydalanib yechamiz:

$$\text{tg}160^\circ = \text{tg}(180^\circ - 20^\circ) = -\text{tg}20^\circ$$

$$\text{tg}140^\circ = \text{tg}(180^\circ - 40^\circ) = -\text{tg}40^\circ$$

$$\text{tg}120^\circ = \text{tg}(180^\circ - 60^\circ) = -\text{tg}60^\circ$$

$$2) \text{tg}20^\circ + \text{tg}40^\circ + \text{tg}60^\circ + \dots$$

$$-\text{tg}60^\circ - \text{tg}40^\circ - \text{tg}20^\circ + \text{tg}180^\circ = 0.$$

Javob: 0.

5.  $2\sin^2\alpha - 1$  ifodani ko'paytma ko'rinishiga keltiring.

**Yechish:**

$2\sin^2\alpha - 1$  ko'paytma ko'rinishida yozamiz:

$$1) 2\sin^2\alpha - 1 = 2\sin^2\alpha - \cos^2\alpha - \sin^2\alpha =$$

$$= \sin^2\alpha - \cos^2\alpha = (\sin\alpha - \cos\alpha)(\sin\alpha + \cos\alpha)$$

$$2) (\sin\alpha - \cos\alpha)(\sin\alpha + \cos\alpha) =$$

$$= \sqrt{2} \left( \frac{\sqrt{2}}{2} \sin\alpha - \frac{\sqrt{2}}{2} \cos\alpha \right) \cdot$$

$$\sqrt{2} \left( \frac{\sqrt{2}}{2} \sin\alpha + \frac{\sqrt{2}}{2} \cos\alpha \right) =$$

$$= 2 \cdot (\sin\alpha \cdot \cos 45^\circ - \sin 45^\circ \cdot \cos\alpha) \cdot$$

$$(\sin\alpha \cdot \cos 45^\circ + \sin 45^\circ \cdot \cos\alpha) =$$

$$= 2\sin(\alpha - 45^\circ) \cdot \sin(\alpha + 45^\circ) =$$

$$= -2\sin(45^\circ - \alpha) \cdot \sin(\alpha + 45^\circ).$$

Javob:  $-2\sin(45^\circ - \alpha) \cdot \sin(\alpha + 45^\circ)$ .

6. Tengsizlikni yeching:

$$\frac{x^2 - 7x - 2}{x^2 + 3x + 2} - \frac{2x - 8}{x + 2} \geq 0.$$

**Yechish:**

$$1) \text{aniqlanish sohasi } x^2 + 3x + 2 \neq 0, x + 2 \neq 0$$

$$(x + 1)(x + 2) \neq 0$$

$$(-\infty; -2) \cup (-2; -1) \cup (-1; \infty)$$

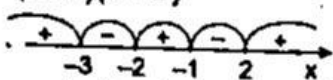
$$2) \frac{x^2 - 7x - 2}{x^2 + 3x + 2} - \frac{2x - 8}{x + 2} \geq 0$$

$$\frac{x^2 - 7x - 2}{(x + 1)(x + 2)} - \frac{2x - 8}{x + 2} \geq 0$$

$$\frac{x^2 - 7x - 2 - 2x^2 - 2x + 8x + 8}{(x + 1)(x + 2)} \geq 0$$

$$\frac{-x^2 - x + 6}{(x+1)(x+2)} \geq 0, \frac{x^2 + x - 6}{(x+1)(x+2)} \leq 0,$$

$$\frac{(x-2)(x+3)}{(x+1)(x+2)} \leq 0$$



$$x \in [-3; -2) \cup (-1; 2].$$

Javob:  $[-3; -2) \cup (-1; 2].$

7. Qarang: 23-variant 28-savol (167-bet).

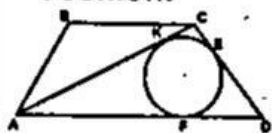
8. Qarang: 23-variant 20-savol (165-bet).

9. ABCD trapetsiyaning AD katta asosi 12 ga teng. ACD uchburchakka aylana ichki chizilgan bo'lib, u CD yon tomonini D uchidan boshlab hisoblaganda 5 va 3 ga teng kesmalarga ajratgan holda urinadi. AC diagonal uzunligini toping.

Berilgan:

ABCD – trapetsiya  
AD = 12  
DE = FD = 5  
CE = 3  
AC = ?

Yechish:



AC = AK + KC  
AK = AF,  
KC = CE = 3

$$AF = AD - FD = 12 - 5 = 7$$

$$AC = 7 + 3 = 10.$$

Javob: 10.

10.  $\frac{2}{|x+1|+1} \leq 2 - |x+1|$  tengsizlikning barcha butun yechimlari yig'indisini toping.

Yechish:

$$\frac{2}{|x+1|+1} \leq 2 - |x+1|$$

1)  $|x+1| = a$  belgilaymiz:

$$\frac{2}{a+1} \leq 2 - a,$$

$$\frac{2 - 2a + a^2 - 2 + a}{a+1} \leq 0$$

$$\frac{a^2 - a}{a+1} \leq 0 \Rightarrow \frac{a(a-1)}{a+1} \leq 0,$$

$$0 \leq a \leq 1.$$

- 2)  $0 \leq |x+1| \leq 1, |x+1| \leq 1,$   
 $-1 \leq x+1 \leq 1, -2 \leq x \leq 0. x \in [-2; 0]$   
 3)  $[-2; 0]$  butun sonlar yig'indisi  
 $-2 - 1 + 0 = -3.$

Javob: -3.

11. Ifoda ning qiymatini toping

$$\frac{2 \cdot 4^{-2} + (3^{-2})^2 \cdot \left(\frac{1}{9}\right)^{-2}}{5^{-3} \cdot 25^2 + (0,7)^0 \cdot \left(\frac{1}{2}\right)^{-2}}$$

$$5^{-3} \cdot 25^2 + (0,7)^0 \cdot \left(\frac{1}{2}\right)^{-2}$$

Yechish:

$$\frac{2 \cdot 4^{-2} + (3^{-2})^2 \cdot \left(\frac{1}{9}\right)^{-2}}{5^{-3} \cdot 25^2 + (0,7)^0 \cdot \left(\frac{1}{2}\right)^{-2}} = \frac{\frac{2}{16} + 3^{-4} \cdot 3^4}{5^{-3} \cdot 5^4 + 2^2} =$$

$$5^{-3} \cdot 25^2 + (0,7)^0 \cdot \left(\frac{1}{2}\right)^{-2}$$

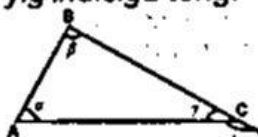
$$\frac{\frac{1}{8} + 1}{5 + 4} = \frac{\frac{9}{8}}{9} = \frac{9}{8 \cdot 9} = \frac{1}{8}$$

Javob:  $\frac{1}{8}.$

12. Quyida keltirilgan jumalardan noto'g'risini toping.

Yechish:

Uchburchakning tashqi burchagi o'ziga qo'shni bo'lmagan ichki burchaklari yig'indisiga teng.



$$\gamma' = \alpha + \beta$$

Javob: uchburchakning tashqi burchagi, ikkita ichki burchaklari yig'indisiga teng.

13. Qarang: 19-variant 30-savol (141-bet).

14.  $\frac{2}{x} + 3 \leq \sqrt{41 - \frac{16}{x}}$  tengsizlikni yeching.

Yechish:

1) aniqlanish sohasi  $x \neq 0$  va  $41 - \frac{16}{x} \geq 0.$

$$\frac{41x - 16}{x} \geq 0, x < 0, x \geq \frac{16}{41}.$$

2) tengsizlikning ikkala qismini kvadratga ko'taramiz:

$$\left(\frac{2}{x} + 3\right)^2 \leq 41 - \frac{16}{x}$$

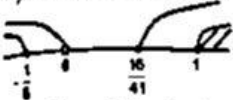
$$\frac{4}{x^2} + \frac{4 \cdot 3}{x} + 9 - 41 + \frac{16}{x} \leq 0$$

$$\frac{4}{x^2} + \frac{28}{x} - 32 \leq 0, \frac{1}{x^2} + \frac{7}{x} - 8 \leq 0$$

$$\frac{-8x^2 + 7x + 1}{x^2} \leq 0, 8x^2 - 7x - 1 \geq 0$$

$$x \leq -\frac{1}{8}, x \geq 1$$

3) tengsizlikning yechimi:



$x < 0$  yoki  $x \geq 1$ .

Javob:  $x < 0$  yoki  $x \geq 1$ .

15. Qarang: 23-variant 7-savol (163-bet).

16.  $y^2 - xy - 2x^2 - 13 = 0$  tenglamaning butun yechimlari nechta?

Yechish:

$y^2 - xy - 2x^2 - 13 = 0$  tenglamani ko'paytuvchilarga ajratamiz:

$$y^2 - x^2 - xy - x^2 = 13$$

$$(y-x)(y+x) - x(y+x) = 13$$

$$(y+x)(y-2x) = 13$$

$(y+x)(y-2x) = 13$  tenglama quyidagi tenglamalar sistemasiga teng kuchli:

$$1) \begin{cases} y+x=1 \\ y-2x=13 \end{cases}; 2) \begin{cases} y+x=13 \\ y-2x=1 \end{cases}$$

$$3) \begin{cases} y+x=-1 \\ y-2x=-13 \end{cases}; 4) \begin{cases} y+x=-13 \\ y-2x=-1 \end{cases}$$

Har bir tenglamalar sistemasini yechib, tenglamaning butun yechimlarini topamiz.

$$1) \begin{cases} y+x=1 \\ y-2x=13 \end{cases}; 2) \begin{cases} y+x=13 \\ y-2x=1 \end{cases}$$

$$3x = -12 \quad 3x = 12$$

$$x = -4 \quad x = 4$$

$$y = 5 \quad y = 9$$

$$(-4; 5) \quad (4; 9)$$

$$3) \begin{cases} y+x=-1 \\ y-2x=-13 \end{cases}; 4) \begin{cases} y+x=-13 \\ y-2x=-1 \end{cases}$$

$$3x = 12 \quad 3x = -12$$

$$x = 4 \quad ; \quad x = -4$$

$$y = -5 \quad y = -9$$

$$(4; -5) \quad (-4; -9)$$

Demak, tenglamaning butun yechimlari:  $(-4; 5), (4; 9), (4; -5), (-4; -9)$  4 ta.

Javob: 4.

17.  $a$  va  $b$  natural sonlarning umumiy bo'luvchilari soni 6 ga teng bo'lsa,  $3a + b$  va  $a$  sonlarning umumiy bo'luvchilari nechta?

Yechish:

$a, b \in \mathbb{N}$ . Umumiy bo'luvchisi 6 bo'lsa, ya'ni  $\tau(EKUB(a; b)) = 6$  bo'lsa,

$\tau(EKUB(3a + b; a)) = 6$  bo'ladi. Masalan:

$$a = 28, b = 84, a = 2^2 \cdot 7,$$

$$b = 2^2 \cdot 7 \cdot 3.$$

$$EKUB(a; b) = 2^2 \cdot 7$$

$$\tau(EKUB(a; b)) = (2+1) \cdot (1+1) = 6$$

$$3a + b = 3 \cdot 28 + 84 = 168 = 2^3 \cdot 3 \cdot 7$$

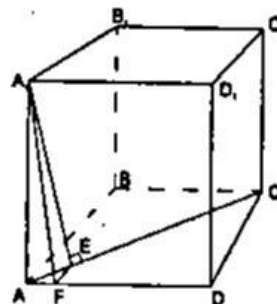
$$EKUB(3a + b; a) = 2^2 \cdot 7$$

$$\tau(EKUB(3a + b; a)) = (2+1) \cdot (1+1) = 6.$$

Javob: 6.

18. Parallelepipedning yoqlari tomoni  $a$  va o'tkir burchagi  $60^\circ$  bo'lgan teng romblardan iborat. Parallelepiped hajmini toping.

Yechish:



$ABCD, B_1C_1D_1$  - parallelepiped. Yoqlari romb.

$$1) ABCD \text{ romb } S_{ABCD} = a^2 \cdot \sin \alpha$$

$$\alpha = 60^\circ, S_{ABCD} = \frac{\sqrt{3}a^2}{2}$$

2)  $A_1E = H, A_1F \perp AD, \Delta A_1AF$  da

$$AF = AA_1 \cdot \cos \alpha = a \cdot \frac{1}{2} = \frac{a}{2}$$

3)  $\Delta AFE$  da  $AF = AE \cdot \cos \frac{\alpha}{2}$

$$AE = \frac{AF}{\cos \frac{\alpha}{2}} = \frac{\frac{a}{2}}{\cos 30^\circ} = \frac{a}{\sqrt{3}}$$

4)  $\Delta A_1AE$  da

$$H = \sqrt{AA_1^2 - AE^2} = \sqrt{a^2 - \left(\frac{a}{\sqrt{3}}\right)^2} =$$

$$= \sqrt{a^2 - \frac{a^2}{3}} = \frac{a\sqrt{2}}{\sqrt{3}}$$

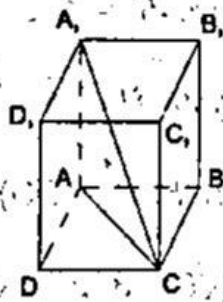
$$5) V = S_{ABCD} \cdot H = \frac{\sqrt{3}a^2}{2} \cdot \frac{a\sqrt{2}}{\sqrt{3}} = \frac{a^3\sqrt{2}}{2} = \frac{a^3}{\sqrt{2}}$$

Javob:  $\frac{a^3}{\sqrt{2}}$

19. To'g'ri parallelepiped diagonallari 9 sm va  $\sqrt{33}$  sm ga teng. Asosining perimetri 18 sm ga teng. Yon qirasi 4 sm ga teng. Parallelepiped to'la sirtini toping.

**Yechish:**

$ABCD A_1 B_1 C_1 D_1$   
to'g'ri parallelepiped  
 $B_1 D_1 = 9$  sm  
 $AC_1 = \sqrt{33}$  sm  
 $AA_1 = 4$  sm  
 $P = 18$  sm  
 $S_{to'la} = ? V = ?$



1)  $BD^2 = B_1 D_1^2 - BB_1^2 = 9^2 - 4^2 = 65$

$BD = d_1 = \sqrt{65}$

$AC^2 = AC_1^2 - CC_1^2 = \sqrt{33^2} - 4^2 = 17$

$AC = d_2 = \sqrt{17}$

2)  $ABCD$  parallelogramm.

$AB = a, BC = b$   
 $2(a + b) = 18, a + b = 9.$

3)  $2(a^2 + b^2) = d_1^2 + d_2^2$

$2(a^2 + b^2) = 65 + 17 = 82$   
 $a^2 + b^2 = 41.$

4)  $\begin{cases} a + b = 9 & a = 5, a = 4 \\ a^2 + b^2 = 41 & \Rightarrow b = 4, b = 5 \end{cases}$

5) Parallelogramm o'tkir burchagini topamiz:  
 $d_2^2 = a^2 + b^2 - 2ab \cdot \cos \alpha$

$$\cos \alpha = \frac{a^2 + b^2 - d_2^2}{2ab} = \frac{4^2 + 5^2 - (\sqrt{17})^2}{2 \cdot 4 \cdot 5} =$$

$$= \frac{16 + 25 - 17}{40} = \frac{24}{40} = \frac{3}{5}$$

$\cos \alpha = \frac{3}{5} \Rightarrow \sin \alpha = \frac{4}{5}$

6)  $S_{asos} = a \cdot b \cdot \sin \alpha = 4 \cdot 5 \cdot \frac{4}{5} = 16$

$S_{to'la} = 2S_{asos} + S_{yon} = 2 \cdot 16 + 18 \cdot 4 = 104.$

Javob:  $S_1 = 104.$

20. Qarang: 16-variant 2-savol (117-bet).

21.  $f^{-1}(x) = \sqrt[3]{x+4}$  bo'lsa  $f(f(2))$  ni toping.

**Yechish:**

$f^{-1}(x) = \sqrt[3]{x+4} \Rightarrow x = \sqrt[3]{f(x)+4},$

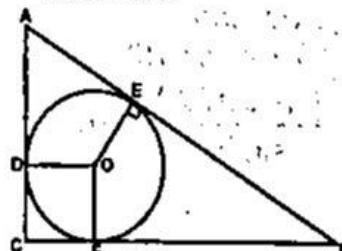
$x^3 = f(x) + 4, f(x) = x^3 - 4$

$f(f(2)) = (f(2))^3 - 4 = (2^3 - 4)^3 - 4 =$   
 $= 64 - 4 = 60.$

Javob: 60.

22. Perimetri 36 sm bo'lgan to'g'ri burchakli uchburchakka aylana ichki chizilgan. Aylananing urinish nuqtasi gipotenuzasi 2:3 nisbatda bo'ladi. Uchburchakning tomonlarini toping.

**Yechish:**



$\Delta ABC$  to'g'ri burchakli,  
 $\angle C = 90^\circ$

$P = 36$  sm,  $AE:EB = 2:3.$

Aylanaga bitta nuqtadan o'tkazilgan urinmalar teng. Shunga ko'ra  $AE = AD,$



$CD = CF, BF = BE, AE = 2x, EB = 3x,$   
 $AB = 5x, CF = r.$   
 1)  $P = 10x + 2r = 36, r + 5x = 18$   
 2)  $(2x + r)^2 + (3x + r)^2 = 25x^2$   
 $13x^2 + 10xr + 2r^2 = 25x^2$   
 $-12x^2 + 10xr + 2r^2 = 0, r = 18 - 5x$   
 $6x^2 - 5xr - r^2 = 0$   
 $(6x + r)(x - r) = 0$   
 $r = -6x, x = r$   
 a)  $r = -6x$  da  $-6x + 5x = 18, x = -18, \emptyset$   
 b)  $r = x$  da  $x + 5x = 18, 6x = 18, x = 3$   
 $r = 3$   
 $AB = 5x = 15$   
 $BC = 3x + r = 9 + 3 = 12$   
 $AC = 2x + r = 6 + 3 = 9$   
 9; 12; 15.

Javob: 12; 9; 15.

23. Qarang: 19-variant 10-savol (137-bet).

24.  $\cos 20^\circ + \cos 40^\circ + \cos 60^\circ + \dots + \cos 160^\circ + \cos 180^\circ$  yig'indisini hisoblang.

Yechish:

1)  $\cos \alpha + \cos 2\alpha + \cos 3\alpha + \dots + \cos n\alpha =$   

$$= \frac{\sin \frac{n\alpha}{2} \cdot \cos \frac{(n+1)\alpha}{2}}{\sin \frac{\alpha}{2}}$$
 formulaga asosan

yechamiz.

2)  $\alpha = 20^\circ, n = 9$

$\cos \alpha + \cos 2\alpha + \dots + \cos n\alpha =$

$$= \frac{\sin \frac{9 \cdot 20^\circ}{2} \cdot \cos \frac{10 \cdot 20^\circ}{2}}{\sin \frac{20^\circ}{2}} = \frac{\sin 90^\circ \cdot \cos 100^\circ}{\sin 10^\circ}$$

3) keltirish formulasiga asosan

$$\cos 100^\circ = \cos(90^\circ + 10^\circ) = -\sin 10^\circ$$

$$4) \frac{\sin 90^\circ \cdot \cos 100^\circ}{\sin 10^\circ} = \frac{1 \cdot (-\sin 10^\circ)}{\sin 10^\circ} = -1.$$

Javob: -1.

25.  $x - 1, 2x + 5, 5x + 1 \dots$  arifmetik progressiya bo'lsa, birinchi 10 ta hadi yig'indisini toping.

Yechish:

1)  $a_1 = x - 1, a_2 = 2x + 5, a_3 = 5x + 1$

Arifmetik progressiya xossasiga ko'ra

$$2a_2 = a_1 + a_3$$

$$2(2x + 5) = x - 1 + 5x + 1$$

$$4x + 10 = 6x, 2x = 10, x = 5. \text{ Bundan } a_1 = 4,$$

$$a_2 = 15, a_3 = 26 \text{ ekanligi kelib chiqadi.}$$

$$2) d = a_2 - a_1 = 11.$$

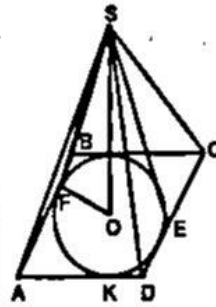
3) yig'indini topamiz:  $S_{10} = \frac{2a_1 + 9d}{2} \cdot 10$

$$S_{10} = 5 \cdot (2 \cdot 4 + 9 \cdot 11) = 5 \cdot 107 = 535.$$

Javob: 535.

26. Piramida asosi tomoni  $4\sqrt{3}$  va o'tkir burchagi  $45^\circ$  ga teng bo'lgan rombdan iborat. Ushbu piramidaga ichki chizilgan konusning yasovchisi bilan  $60^\circ$  li burchak tashkil etadi. Konusning hajmini toping.

Yechish:



SABCD – piramida,

ABCD – romb

$$AB = 4\sqrt{3}, SO = H,$$

$$\angle BAD = 45^\circ$$

$\Delta SOF$  to'g'ri burchakli.

$$\angle SFO = 60^\circ$$

$$FO = \frac{h}{2}$$

$$h = AB \cdot \sin 45^\circ = 4\sqrt{3} \cdot \frac{\sqrt{2}}{2} = 2\sqrt{6}, FO = \sqrt{6}$$

$$\frac{H}{FO} = \operatorname{tg} 60^\circ, H = \sqrt{6} \cdot \sqrt{3} = 3\sqrt{2}$$

$$V_k = \frac{1}{3} \pi r^2 H = \frac{1}{3} \pi (FO)^2 \cdot H =$$

$$= \frac{1}{3} \pi \cdot (\sqrt{6})^2 \cdot 3\sqrt{2} = 6\sqrt{2}\pi$$

Javob:  $6\sqrt{2}\pi$ .

27.  $y = x^2 - 6x + 7$  parabola va  $y = -x^2 - 4x - 5$  parabola uchlaridan o'tuvchi to'g'ri chiziq tenglamasini tuzing.

Yechish:

$$y = x^2 - 6x + 7, y = -x^2 - 4x - 5$$

$$1) y = x^2 - 6x + 7, x_0 = -\frac{b}{2a} = \frac{6}{2} = 3,$$

$$y_0 = 9 - 18 + 7 = -2.$$

$$A(3; -2)$$

2)  $y = -x^2 - 4x - 5,$

$x_0 = \frac{-b}{2a} = \frac{-4}{2} = -2,$

$y_0 = -4 + 8 - 5 = -1. B(-2; -1)$

3) A(3; -2), B(-2; -1) nuqtalardan o'tuvchi to'g'ri chiziq tenglamasi tuzamiz.

$y = kx + b.$

$$\begin{cases} -2 = 3k + b \\ -1 = -2k + b \end{cases} \Rightarrow \begin{cases} k = -\frac{1}{5} \\ b = -\frac{7}{5} \end{cases}$$

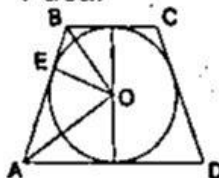
4)  $y = -\frac{x}{5} - \frac{7}{5}.$

Javob:  $-\frac{x}{5} - \frac{7}{5}.$

28. Teng yonli trapetsiyaga ichki chizilgan aylana markazidan trapetsiyaning yon tomonining uchlarigacha bo'lgan masofa mos ravishda 9 va 12 sm ga teng. Trapetsiya yuzasini toping.

Yechish:

I-usul



ABCD teng yonli trapetsiya.  
 $AD + BC = AB + CD,$   
 chunki aylana ichki chizilgan

$BO = 9, AO = 12$   
 $S = ?$

1)  $S = \frac{a+b}{2} \cdot h, AD = a, BC = b, h = 2r.$

$\Delta AOB$  to'g'ri burchakli

$OE = r = \frac{BO \cdot AO}{AB}$

$AB^2 = BO^2 + AO^2 = 9^2 + 12^2 = 15^2$

$AB = 15.$

$r = \frac{9 \cdot 12}{15} = \frac{36}{5} = 7,2.$

$h = 14,4.$

2)  $(\frac{b}{2})^2 = 9^2 - 7,2^2 = (9 + 7,2)(9 - 7,2) = 16,2 \cdot 1,8$

$(\frac{b}{2}) = 5,4 \rightarrow 10,8$

$(\frac{a}{2})^2 = 12^2 - 7,2^2 =$

$= (12 - 7,2)(12 + 7,2) = 4,8 \cdot 19,2.$

$(\frac{a}{2}) = 9,6 \rightarrow a = 19,2$

$S = \frac{10,8 + 19,2}{2} \cdot 14,4 = 216$

II-usul

$x = 9$

$y = 12$

$S_1 = ?$



1)  $a + b = 2c, c = \frac{a+b}{2}$

$r = \frac{xy}{c}, h = 2r$

2)  $c^2 = x^2 + y^2 = 9^2 + 12^2 = 15^2$   
 $c = 15$

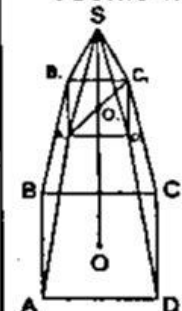
3)  $r = \frac{9 \cdot 12}{15} = \frac{36}{5}$

4)  $S = \frac{a+b}{2} \cdot h = c \cdot 2r = 2 \cdot 15 \cdot \frac{36}{5} = 2 \cdot 3 \cdot 36 = 216.$

Javob: 216.

29. To'g'ri burchakli muntazam piramidaning asosiga parallel bo'lgan va piramida balandligini 1:3 nisbatda bo'luvchi tekislik o'tkazildi. Hosil bo'lgan kesimning diagonali 3 ga teng bo'lsa, piramidaning asos tomonini toping.

Yechish:



SABCD muntazam to'rtburchakli piramida  
 $ABCD \parallel A_1B_1C_1D_1$   
 $A_1C_1 = 3$   
 $SO_1 : SO = 1 : 3$   
 $AB = ?$

1)  $A_1C_1^2 = A_1D_1^2 + C_1D_1^2$

$A_1D_1 = a$

$2a^2 = 3^2, a = \frac{3}{\sqrt{2}}$

2)  $SO_1 = x, OO_1 = 3x, SO = 4x$



3)  $\Delta A_1SC_1$  va  $\Delta ASC$  o'xshash.

$$\frac{SO_1}{AC_1} = \frac{SO}{AC}, \frac{x}{3} = \frac{4x}{AC}, AC = 12.$$

4)  $AC^2 = AD^2 + CD^2, AD = b$

$$12^2 = b^2 + b^2 = 2b^2, \sqrt{2} b = 12, b = \frac{12}{\sqrt{2}} = 6\sqrt{2}.$$

Javob:  $6\sqrt{2}$ .

30. Silindr yon sirti 1 ga teng. Silindr balandligi 6 marta kattalashtirilsa, asosining radiusi esa 3 marta kichraytirilsa, ushbu silindr yon sirtini toping.

31. Qarang: 22-variant 32-savol (160-bet).

32. Qarang: 21-variant 36-savol (155-bet).

33. Qarang: 17-variant 35-savol (129-bet).

34. A="BIOS – ma'lumotlarni kiritish-chiqarish sistemasini kengaytirish modulidir."  
 B="Shareware – qiymati 100% to'langandan keyin o'rnatilib, foydalaniladigan dasturiy ta'minot."  
 C="Doppix dasturi ma'lumotlar omborini boshqarish sistemasidir." Shu mulohazalar asosida quyidagi mantiqiy ifodaning natijasini toping:  $\neg(A \vee (\neg B \wedge C))$

Yechish:

A="BIOS – ma'lumotlarni kiritish-chiqarish sistemasini kengaytirish modulidir." – rost (1);

B="Shareware – qiymati 100% to'langandan keyin o'rnatilib, foydalaniladigan dasturiy ta'minot." – yolg'on (0);

C="Doppix dasturi ma'lumotlar omborini boshqarish sistemasidir." – yolg'on (0).

$$\neg(A \vee (\neg B \wedge C)) = \neg(1 \vee (\neg 0 \wedge 0)) = \neg(1 \vee (1 \wedge 0)) = \neg(1 \vee 0) = \neg 1 = 0$$

Javob: yolg'on.

35. Fayl atributi nima?

Yechish:

Fayl atributi har bir fayl uchun o'rnatiladi va tizimga ushbu fayl bilan qanday operatsiyalar bajarish mumkinligi to'g'risida ma'lumot beradi. Fayllarning 4 xil atributi bo'ladi:

— только чтение (R) – faqat o'qish uchun;

— архивный (A) – arxivlangan;

— скрытый (H) – yashirilgan;

— системный (S) – tizimli.

Javob: faqat o'qish uchun, arxivlangan, yashirilgan, tizimli.

36. Qarang: 6-variant 32-savol (51-bet).

Yechish:

$$S_{yon} = 1$$

$$H_1 = 6H$$

$$R_1 = \frac{R}{3}$$

$$S_1 = ?$$

$$S_{yon} = 2\pi RH = 1$$

$$S_1 = 2\pi R_1 H_1 = 2\pi \cdot \frac{R}{3} \cdot 6H = 2\pi RH \cdot 2 =$$

$$= 1 \cdot 2 = 2.$$

Javob: 2.