

# **2017-yıl matematika variant yechimlari (spectrum)**

## **23-variant**

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### 23-variant

1.  $\begin{cases} \log_3(x^2 + y^2) = 3 \\ \log_3 x + \log_3 y = 0 \end{cases}$  tenglamalar  
sistemasining barcha yechimlari  
ko'paytmasini toping.

Yechish:

$$1) \begin{cases} \log_3(x^2 + y^2) = 3 \\ \log_3 x + \log_3 y = 0 \end{cases} \Rightarrow \begin{cases} x^2 + y^2 = 3^3 \\ \log_3 xy = 0 \end{cases} \Rightarrow$$

$$\Rightarrow \begin{cases} x^2 + y^2 = 27 \\ xy = 3 \end{cases} \Rightarrow \begin{cases} x^2 + y^2 = 27 \\ xy = 1 \end{cases} \Rightarrow$$

$$\Rightarrow \begin{cases} x = \frac{1}{y} \\ \frac{1}{y^2} + y^2 = 27 \end{cases}$$

$$y^4 - 27y^2 + 1 = 0.$$

$$y^2 = a, a \geq 0.$$

$$a^2 - 27a + 1 = 0.$$

$$a_{1,2} = \frac{27 \pm \sqrt{27^2 - 4}}{2} = \frac{27 \pm 5\sqrt{29}}{2}$$

$$a_1 = \frac{27 + 5\sqrt{29}}{2},$$

$$a_2 = \frac{27 - 5\sqrt{29}}{2}$$

$$y^2 = \frac{27 + 5\sqrt{29}}{2}$$

$$y_{1,2} = \pm \sqrt{\frac{27 + 5\sqrt{29}}{2}}$$

$$y^2 = \frac{27 - 5\sqrt{29}}{2}$$

$$y_{3,4} = \pm \sqrt{\frac{27 - 5\sqrt{29}}{2}}$$

$$y > 0 \text{ bo'lganligi sababli } y = \sqrt{\frac{27 + 5\sqrt{29}}{2}},$$

$$y = \sqrt{\frac{27 - 5\sqrt{29}}{2}}$$

$x > 0$  bo'lganligi sababli

$$x = \frac{\sqrt{2}}{\sqrt{27 + 5\sqrt{29}}}, x = \frac{\sqrt{2}}{\sqrt{27 - 5\sqrt{29}}}$$

Sistema 2 ta yechimga ega. Barcha yechimlari ko'paytmasi

$$\frac{\sqrt{2}}{\sqrt{27 + 5\sqrt{29}}} \cdot \frac{\sqrt{27 + 5\sqrt{29}}}{\sqrt{27 - 5\sqrt{29}}} = 2$$

$$\frac{\sqrt{2}}{\sqrt{27 - 5\sqrt{29}}} \cdot \frac{\sqrt{27 - 5\sqrt{29}}}{\sqrt{27 + 5\sqrt{29}}} = 1$$

Javob: 1.

2. Hisoblang:  $\sin 45^\circ \cdot \sin 15^\circ \cdot \cos 165^\circ$ .

Yechish:

$$1) \cos 165^\circ = \cos(180^\circ - 15^\circ) = -\cos 15^\circ$$

$$2) \sin 15^\circ \cdot \cos 165^\circ = -\sin 15^\circ \cdot \cos 15^\circ =$$

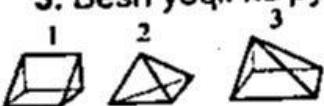
$$= -\frac{1}{2} \cdot 2\sin 15^\circ \cos 15^\circ = -\frac{1}{2} \sin 2 \cdot 15^\circ =$$

$$= -\frac{1}{2} \sin 30^\circ = -\frac{1}{4}$$

$$3) \sin 45^\circ \cdot \left(-\frac{1}{4}\right) = \frac{\sqrt{2}}{2} \cdot \left(-\frac{1}{4}\right) = -\frac{\sqrt{2}}{8}$$

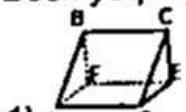
Javob:  $-\frac{\sqrt{2}}{8}$ .

3. Besh yoqli ko'pyoq(lar)ni aniqlang.

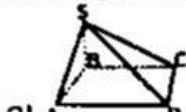


Yechish:

Besh yoqli ko'pburchaklar



1) ABCD, BCEF, AFED, ABF, CED – 5 ta yoq.



3) SBA, SBC, SCD, SAD, ABCD – 5 ta yoq.

Javob: 1, 3.

4.  $\left| \frac{x}{y} \right| < 1$  bo'lsa,  $\frac{x}{y} + \frac{x^2}{y^2} + \frac{x^3}{y^3} + \dots$  ni hisoblang.

Yechish:

$$1) b_1 = \frac{x}{y}, b_2 = \frac{x^2}{y^2}$$

$$q = \frac{b_2}{b_1} = \frac{x^2}{y^2} \cdot \frac{y}{x} = \frac{x}{y} < 1 \text{ bo'lganligi uchun}$$

cheksiz kamayuvchi geometrik progressiya bo'ladi.

2) yig'indini hisoblaymiz:

$$S = \frac{b_1}{1-q}$$

$$S = \frac{\frac{x}{y}}{1 - \frac{x}{y}} = \frac{x}{y} \cdot \frac{y}{y-x} = \frac{x}{y-x}$$

Javob:  $\frac{x}{y-x}$ .

5.  $(x_0, y_0)$  quyidagi tenglamalar sistemasining yechimi bo'lsa,  $x_0^2 + y_0^3$  ni

toping:  $\begin{cases} y - 2 = \sqrt{x} \\ \sqrt{x - 3} = y - 3 \end{cases}$

Yechish:

1) aniqlanish sohasi  $\begin{cases} y - 2 \geq 0 \\ y - 3 \geq 0 \\ x \geq 0 \\ x - 3 \geq 0 \end{cases} \Rightarrow \begin{cases} y \geq 3 \\ x \geq 3 \end{cases}$

2)  $\begin{array}{r} y - 2 = \sqrt{x} \\ y - 3 = \sqrt{x - 3} \\ \hline 1 = \sqrt{x} - \sqrt{x - 3} \end{array}$

$\sqrt{x - 3} = \sqrt{x} - 1$ ,  
 $(\sqrt{x - 3})^2 = (\sqrt{x} - 1)^2$ ,  
 $x - 3 = x - 2\sqrt{x} + 1$ ,  $2\sqrt{x} = 4$ ,  $\sqrt{x} = 2$ ,  $x = 4$ .

3)  $y - 2 = 2$ ,  $y = 4$ . (4; 4)

4)  $x_0^2 + y_0^3 = 4^2 + 4^3 = 16 + 64 = 80$ .

Javob: 80.

6. Bir guruh bolalarning o'rtacha og'irligi 40 kg ga teng. Qiz bolalarning o'rtacha og'irligi 35 kg, o'g'il bolalaming o'rtacha og'irligi esa 50 kg ligi ma'lum. Agar guruh a'zolarining 9 nafari o'g'il bolalar bo'lsa, qiz bolalar sonini toping.

Yechish:

$$\frac{a_1 + a_2 + \dots + a_n}{n} = 40 \text{ guruh bolalari}$$

$$\frac{b_1 + b_2 + \dots + b_m}{m} = 35 \text{ qizlar}$$

$$\frac{c_1 + c_2 + \dots + c_k}{k} = 50 \text{ o'g'il bolalar}$$

$$k = ? m = ?$$

$$n = k + m$$

$$a_1 + a_2 + \dots + a_n = b_1 + b_2 + \dots + b_m +$$

$$+ c_1 + c_2 + \dots + c_k$$

$$k = 9 \text{ da } c_1 + c_2 + \dots + c_9 = 50 \cdot 9$$

$$b_1 + b_2 + \dots + b_m + c_1 + c_2 + \dots + c_9 =$$

$$= 35m + 50 \cdot 9$$

$$40 \cdot (9 + m) = 35m + 50 \cdot 9$$

$$40m - 35m = 50 \cdot 9 - 40 \cdot 9$$

$$5m = 10 \cdot 9, m = 18$$

Qizlar soni 18 nafar.

Javob: 18.

7.  $\bar{a}(x + y; 2 - x), \bar{b}(y - 2x; 1)$

$2\bar{a} + \bar{b} = (3; 3)$  bo'lsa,  $(x; y)$  ni toping.

Yechish:

$$\bar{a}(\bar{a}_1, \bar{a}_2), \bar{b}(\bar{b}_1, \bar{b}_2)$$

$$\bar{a} + \bar{b} = (\bar{a}_1 + \bar{b}_1; \bar{a}_2 + \bar{b}_2)$$

1)  $2\bar{a}(2x + 2y; 4 - 2x)$

2)  $2\bar{a} + \bar{b} = (2x + 2y; 4 - 2x) + (y - 2x; 1) =$

$$= (2x + 2y + y - 2x;$$

$$4 - 2x + 1) = (3y; 5 - 2x)$$

$$3) (3y; 5 - 2x) = (3; 3)$$

$$3y = 3, y = 1$$

$$5 - 2x = 3, x = 1$$

$$(1; 1)$$

Javob:  $(x; y) = (1; 1)$

8.  $|2x - 1| = x$  tenglama yechimlari sonini toping. Bu yerda  $|a|$  – a sonning butun qismi.

Yechish:

[a] – a sonning butun qismi.

$$[2x - 1] = x$$

1)  $x \leq 2x - 1 \leq x + 1$

2)  $x \leq 2x - 1, -x \leq -1, x \geq 1$

3)  $2x - 1 < x + 1, x < 2$

4)  $1 \leq x < 2$  tengsizlik  $x = 1$  dan iborat

yagona butun yechimiga ega.

Javob: 1 ta.

9.  $(x^2 - x - 3)^2 - (x^2 - x - 3) - 3 = x$

tenglamaning butun yechimlari ko'paytmasini toping.

**Yechish:**

$$\begin{aligned} (x^2 - x - 3)^2 - (x^2 - x - 3) - 3 &= x \\ (x^2 - x - 3)^2 - x^2 + x + 3 - 3 - x &= 0 \\ (x^2 - x - 3)^2 &= x^2 \\ |x^2 - x - 3| &= |x|, x^2 - x - 3 = \pm x \\ a) x^2 - x - 3 &= x, x^2 - 2x - 3 = 0, \\ x = -1, x = 3 & \\ b) x^2 - x - 3 &= -x, x^2 - 3 = 0, x^2 = 3, \\ x = \pm\sqrt{3} & \end{aligned}$$

Tenglamaning yechimlari  $x = -1, x = 3$ ,  $x = \pm\sqrt{3}$ . Butun yechimlari  $-1$  va  $3$ . Butun yechimlari ko'paytmasi  $-3$ .

Javob:  $-3$ .**10. Qarang: 9-variant 30-savol (73-bet).**

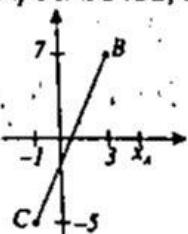
11. ABC teng yonli uchburchakda B(3; 7), C(-1; -5), A uchi koordinata o'qida. A uchning koordinatalarini toping.

**Berilgan:**

$$\begin{aligned} \Delta ABC \\ AB = BC \\ B(3; 7), (-1; -5) \\ A - \text{koordinatalar} \\ \text{o'qida} \\ A(x; y) - ? \end{aligned}$$

**Yechish:**

$$\begin{aligned} A \text{ nuqta OX o'qida} \\ \text{bo'lsa}, A(x; 0), OY \\ \text{oqida bo'lsa}, A(0; y). \end{aligned}$$



Shartiga ko'ra:

$$AB = AC$$

$$\begin{aligned} \Rightarrow \sqrt{(x_B - x_A)^2 + (y_B - y_A)^2} &= \\ = \sqrt{(x_C - x_A)^2 + (y_C - y_A)^2} & \\ (x - 3)^2 + 49 &= (x + 1)^2 + 25 \\ x^2 - 6x + 9 + 49 &= x^2 + 2x + 1 + 25 \Rightarrow \\ 8x = 32, x = 4 & \end{aligned}$$

Demak, A nuqtanining koordinatalari A(4; 0).

Javob: (4; 0).

**12. Tenglamani yeching:**

$$\sqrt{6^{x+2} - 2} = 8 - 36 \cdot 6^x$$

**Yechish:**

$$\sqrt{6^{x+2} - 2} = 8 - 6^{x+2}$$

$$\begin{aligned} \sqrt{6^{x+2} - 2} &\geq 0 \text{ bo'lganligi uchun} \\ 6^{x+2} - 2 &\geq 0 \text{ bo'ladi } 6^{x+2} \leq 8. \\ 6^{x+2} &= a \text{ deb belgilaymiz.} \end{aligned}$$

$$\sqrt{a - 2} = 8 - a \text{ tenglamani yechamiz.}$$

$$\begin{cases} a - 2 \geq 0 \\ 8 - a \geq 0 \end{cases} \Rightarrow 2 \leq a \leq 8$$

$$a - 2 = (8 - a)^2$$

$$a - 2 = 64 - 16a + a^2,$$

$$a^2 - 17a + 66 = 0.$$

$$a = 6, a = 11.$$

$2 \leq a \leq 8$  bo'lganligi uchun tenglamaning ildizi  $a = 6$  bo'ladi.

$$6^{x+2} = 6.$$

$$x + 2 = 1, x = -1.$$

Javob:  $-1$ .

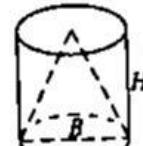
13. Silindr va konus umumiy asosga va balandlikka ega. Silindr hajmi 9 ga teng. Konus hajmini toping.

**Yechish:**

$$H = 2R = 2r$$

$$V = 9$$

$$V_k = ?$$



$$1) V = \pi R^2 H = 2\pi R^3 = 9$$

$$2) V_k = \frac{1}{3} \pi R^2 H = \frac{2\pi R^3}{3} = \frac{9}{3} = 3$$

Javob: 3.

**14. Qarang: 4-variant 13-savol (30-bet).**

15.  $y = \frac{x^3 + 1}{x + 1}$  funksiyanining eng kichik butun qiymatini toping.

**Yechish:**

$$y = \frac{x^3 + 1}{x + 1}, x \neq -1$$

Qisqa ko'paytirish formulasiga asosan

$$y = \frac{x^3 + 1}{x + 1} = \frac{(x + 1)(x^2 - x + 1)}{x + 1} =$$

$$= x^2 - x + 1 = (x - 0,5)^2 + \frac{3}{4}$$

Funksiyanining eng kichik qiymati 1.

Javob: 1.

16. Agar  $\int (3x^2 + 1)dx = 36$  va  $a^2 + ab + b^2 = 17$  bo'lsa,  $b - a$  ni toping.

Yechish:

1) Integralni hisoblaymiz.

$$\int (3x^2 + 1)dx = \left( \frac{3x^3}{2+1} + x \right) \Big|_a^b = \\ = (x^3 + x) \Big|_a^b = b^3 + b - a^3 - a$$

$$\begin{aligned} 2) b^3 + b - a^3 - a &= (b^3 - a^3) + (b - a) = \\ &= (b - a)(b^2 + ab + a^2) + (b - a) = \\ &= (b - a)(b^2 + ab + a^2 + 1) = \\ &= (b - a)(17 + 1) = 18(b - a) \\ 3) 18(b - a) &= 36, b - a = 2. \end{aligned}$$

Javob: 2.

17. Qarang: 4-variant 6-savol (29-bet).

18.  $\bar{a}(-2; 3)$  va  $\bar{b}(2; n)$  vektorlar berilgan.  $n$  ning qanday qiymatida bu vektorlar o'zaro perpendikulyar bo'ladi?

Yechish:

$\bar{a}(-2; 3)$ ,  $\bar{b}(2; n)$ ,  $\bar{a} \perp \bar{b}$ ,  $n = ?$

$\bar{a} \perp \bar{b}$  bo'lishi uchun  $\bar{a} \cdot \bar{b} = 0$  bo'lishi kerak.  
 $\bar{a} \cdot \bar{b} = (-2; 3) \cdot (2; n) = -2 \cdot 2 + 3 \cdot n = 0$

$$-4 + 3n = 0, n = \frac{4}{3}.$$

Javob:  $\frac{4}{3}$ .

19. Tenglamani yeching:

$$\sqrt{x} + \frac{3}{\sqrt{5+x}} = \sqrt{5+x}.$$

Yechish:

1) aniqlanish sohasi,  $x \geq 0$ ,  
 $x > -5 \Rightarrow x \geq 0$ .

$$2) \sqrt{x(5+x)} + 3 = 5 + x$$

$$\sqrt{5x+x^2} = 2 + x, x + 2 \geq 0, x \geq -2$$

$$5x + x^2 = 4 + 4x + x^2$$

$$x = 4.$$

Javob: 4.

20.  $x$  va  $y$  quyidagi tenglamalar sistemasining yechimlari bo'lsa,  $x \cdot y$  qiymatini toping.

$$\begin{cases} 0,2^x - 2^{0,5y} = 3 \\ 0,04^x - 2^y = 21 \end{cases}$$

Yechish:

$$\begin{cases} 0,2^x - 2^{0,5y} = 3 \\ 0,04^x - 2^y = 21 \end{cases}$$

$$x \cdot y = ?$$

$$1) \begin{cases} 5^{-x} - 2^{0,5y} = 3 \\ 5^{-2x} - 2^y = 21 \end{cases} 5^{-x} = a, 2^{0,5y} = b.$$

$$2) \begin{cases} a - b = 3 \\ a^2 - b^2 = 21 \end{cases} \Rightarrow \begin{cases} a - b = 3 \\ (a - b)(a + b) = 21 \end{cases} \Rightarrow$$

$$\Rightarrow \begin{cases} a - b = 3 \\ a + b = 7 \end{cases} \Rightarrow \begin{cases} a = 5 \\ b = 2 \end{cases}$$

$$3) 5^{-x} = 5, -x = 1, x = -1. \\ 2^{0,5y} = 2, 0,5y = 1, y = 2.$$

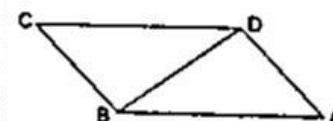
$$(-1; 2)$$

$$3) x \cdot y = -1 \cdot 2 = -2.$$

Javob: -2.

21. ABCD parallelogrammda  $|BC| = 2$ ,  $|DC| = 4$ ,  $\angle DAB = 60^\circ$  bo'lsa,  $|BD|$  ni toping.

Yechish:



ABCD parallelogram  $\angle DAB = 60^\circ$ ,  $BC = 2$ ,  $DC = 4$ ,  $BD$  diagonalni kosinuslar teoremasidan foydalanib topamiz.  
 $BD^2 = AB^2 + AD^2 - 2AB \cdot AD \cdot \cos A$   
 $BD^2 = 4^2 + 2^2 - 4 \cdot 2 \cos 60^\circ$   
 $BD^2 = 16 + 4 - 8 = 12$   
 $BD = 2\sqrt{3}$ .

Javob:  $2\sqrt{3}$ .

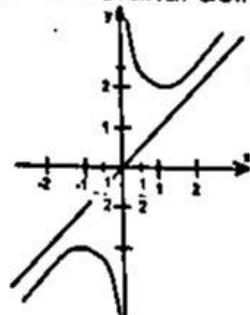
22.  $y = \frac{x^2 + 1}{x}$  funksiyanining qiymatlari

sohasiga tegishli bo'lmagan butun sonlar yig'indisini toping.

**Yechish:**

$$y = \frac{x^2 + 1}{x}, x \neq 0.$$

Funksiya grafigini yasaymiz.  
 $x = 0$  vertikal asimptota.



$$K = \lim_{x \rightarrow \infty} \frac{y}{x} = \lim_{x \rightarrow \infty} \frac{x^2 + 1}{x^2} = \lim_{x \rightarrow \infty} \left(1 + \frac{1}{x^2}\right) = 1$$

$$b = \lim_{x \rightarrow \infty} (y - kx) = \lim_{x \rightarrow \infty} \left( \frac{x^2 + 1}{x} - x \right) = 0$$

$y = x$  og'ma asimptota.

Funksiyaning qiymatlar sohasi:

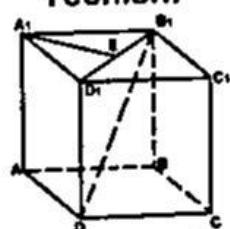
$(-\infty; -2] \cup [2; \infty)$ .

Qiymatlar sohasiga tegishli bo'lmagan oraliq  $(-2; 2)$ . Butun sonlar  $-1, 0, 1$ .

Yig'indisi  $-1 + 0 + 1 = 0$ .

Javob: 0.

23. Kubning diagonalidan ushbu diagonal bilan kesishmaydigan qirrasigacha bo'lgan masofa 2 ga teng. Kubning hajmini toping.

**Yechish:**

$ABCDA_1B_1C_1D_1$  - kub,  
 $AB = a$ ,  
 $B_1D$  - diagonal,  
 $AA_1$  qirradan  $B_1D$   
diagonalgacha bo'lgan  
masofa  $AA_1$  qirradan  
 $BB_1D_1D$

tekislikkacha bo'lgan masofaga teng,  
bu masofa  $A_1E$  kesma uzunligiga teng..

$A_1E = 2$ ,  $V = ?$

$$A_1E^2 = A_1B_1^2 - B_1E^2$$

$$2^2 = a^2 - \left(\frac{a\sqrt{2}}{2}\right)^2 = \frac{a^2}{2}, a = 2\sqrt{2}$$

$$V = a^3 = (2\sqrt{2})^3 = 16\sqrt{2}$$

Javob:  $16\sqrt{2}$ .

24.  $x$  va  $y$  quyidagi tenglamalar sistemasining yechimlari bo'lsa,  $|x + y|$  qiymatini toping.

$$\begin{cases} 5^{2x} - (0,25)^y = 21 \\ 5^x - (0,5)^y = 3 \end{cases}$$

**Yechish:**

$$\begin{cases} 5^{2x} - (0,25)^y = 21 \\ |x + y| = ? \end{cases}$$

$$\begin{cases} 5^x - (0,5)^y = 3 \\ 5^{2x} - 2^{-2y} = 21 \end{cases}$$

$$1) \begin{cases} 5^x - 2^{-y} = 3 \\ 5^{2x} - 2^{-2y} = 21 \end{cases}$$

$$5^x = a, 2^{-y} = b.$$

$$2) \begin{cases} a^2 - b^2 = 21 \\ a - b = 3 \end{cases} \Rightarrow \begin{cases} (a-b)(a+b) = 21 \\ a - b = 3 \end{cases} \Rightarrow$$

$$\Rightarrow \begin{cases} a+b = 7 \\ a-b = 3 \end{cases} \Rightarrow \begin{cases} a = 5 \\ b = 2 \end{cases}$$

$$3) 5^x = 5, x = 1$$

$$2^{-y} = 2, -y = 1, y = -1.$$

$$(1; -1)$$

$$4) |x + y| = |1 + (-1)| = 0.$$

Javob: 0.

25.  $(x_0, y_0)$  quyidagi tenglamalar

sistemmasining yechimi bo'lsa,  $\frac{x_0}{y_0}$  ni toping:

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - y = 1 \end{cases}$$

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - 1 = y \end{cases}$$

**Yechish:**

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - 1 = y \end{cases} \text{ sistemani qo'shish usuli bilan}$$

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - 1 = y \end{cases} \text{ yechamiz.}$$

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - 1 = y \end{cases} \quad \begin{aligned} &\sqrt{x} + \sqrt{y} = 3 \\ &+ \sqrt{x} - 1 = y \end{aligned}$$

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - 1 = y \end{cases} \quad \begin{aligned} &2\sqrt{x} = 4, \sqrt{x} = 2; x = 4 \\ &\sqrt{y} = 1, y = 1. (4; 1) \end{aligned}$$

$$\begin{cases} \sqrt{x} + \sqrt{y} = 3 \\ \sqrt{x} - 1 = y \end{cases} \quad \begin{aligned} &\frac{x_0}{y_0} = \frac{4}{1} = 4 \end{aligned}$$

Javob: 4.

26. Agar  $f(x) = mx^2 - (m - 14)x - 2$  parabolaning simmetriya o'qi tenglamasi  $x = -3$  bo'lса,  $m$  ning qiymatini toping.

**Yechish:**

$$f(x) = mx^2 - (m - 14)x - 2.$$

$$\text{Simmetriya o'qi tenglamasi } x = -\frac{b}{2a} \text{ yoki}$$

$$x = \frac{m-14}{2m}.$$

Misol shartiga ko'ra:  $x = -3$ , bundan

$$\frac{m-14}{2m} = -3, m - 14 = -6m$$

$$7m = 14, m = 2.$$

**Javob:** 2.

27. Agar  $a < 0$  va  $b > 0$  bo'lса,  $ax + a > bx + b$  tengsizlikni yeching.

**Yechish:**

$a < 0, b > 0$  bo'lса,  $ax + a > bx + b$  tengsizlikni yechamiz.

$$ax + a > bx + b$$

$$bx - ax < -b + a$$

$$x(b - a) < -b + a$$

$a < 0, b > 0$  bo'lganligi uchun  $b - a > 0$

$$x < \frac{-b+a}{b-a} = \frac{-(b-a)}{b-a} = -1, x < -1.$$

**Javob:**  $x < -1$ .

28. ABC uchburchakda C burchagi  $90^\circ$  ga teng,  $AC = 20$ ,  $BC = 14$ .  $\tg A$  ni toping.

31. Qarang: 8-variant 32-savol (66-bet).

32. Qarang: 7-variant 34-savol (58-bet).

33. A="MSDOS.SYS – operatsion sistemani faollashtiruvchi dastur." B="Biror nomga ega bo'lgan va kompyuter tashqi xotirasida joylashgan baytlar majmuiga katalog deyiladi."

C="Brainware – kompyuter tomonidan ishlataladigan barcha dasturlar to'plamidir." Shu mulohazalar asosida quyidagi mantiqiy ifodaning natijasini toping:

C and not (A or B)

**Yechish:**

Mulohazalarni tahlil qilamiz:

A="MSDOS.SYS – operatsion sistemani faollashtiruvchi dastur." – rost (1)

**Yechish:**

$\Delta ABC$  to'g'ri burchakli  
 $\angle C = 90^\circ$   
 $AC = 20$   
 $BC = 14$   
 $\tg A = ?$

O'tkir burchak tangensiga ko'ra

$$\tg A = \frac{CB}{AC} = \frac{14}{20} = 0,7$$

**Javob:** 0,7.

29. Qarang: 4-variant 4-savol (28-bet).

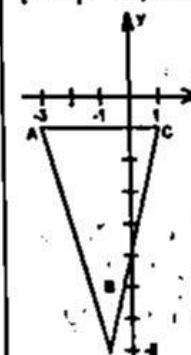
30. A(-3; -1), B(-1; -8), C(1; -1) nuqtalarini tutashtirishdan hosil bo'lgan uchburchak yuzini toping.

**Yechish:**

A(-3; -1), B(-1; -8), C(1; -1)

$\Delta ABC$  teng yonli, AC – asos.

$|AC| = 4, BD$  – balandlik,  $|BD| = 7$



$$S = \frac{|AC| \cdot |BD|}{2} = \frac{4 \cdot 7}{2} = 14$$

**Javob:** 14.

B="Biror nomga ega bo'lgan va kompyuter tashqi xotirasida joylashgan baytlar majmuyiga katalog deyiladi." – yolg'on (0)  
 C="Brainware – komyuter tomonidan ishlataladigan barcha dasturlar to'plamidir." – yolg'on.  
 $C \text{ and not } (A \text{ or } B) = 0 \text{ and not } (1 \text{ or } 0) = 0 \text{ and not } 1 = 0 \text{ and } 0 = 0.$

Javob: yolg'on.

**34.** Paskal tilida yozilgan dastur natijasini aniqlang.

```
Var k: byte; S:string; B:array[1..11] of byte;
Begin Randomize; S:='INFORMATIKA';
k:=1; b[k]:=1+Random(1)+Random(1);
While k<b[k]+2 Do begin k:=k+3;
b[k]:=b[k-3]+2; Write(S[b[k]]); end;
Readln; End
```

**Yechish:**

Dasturda  $k = 0..255$  diapazondagi butun o'zgaruchi; S – satr va  $b = 11$  ta  $0..255$  diapazondagi butun sondan iborat massivdan foydalanilgan.

Randomize – tasodifiy sonlar generatori.

```
s:='INFORMATIKA';
k:=1; b[k]:=1+Random(1)+Random(1); { random(1) 0 qiymatni, qabul qiladi. Demak, b[1]=1 bo'ladi}
While k<b[k]+2 Do {Toki k<b[k]+2 bajar: }
begin k:=k+3;
  b[k]:=b[k-3]+2;
  Write(S[b[k]]); { S[b[k]] qiymatini ekranda aks ettir}
```

end;

Batafsilroq while operatorini ko'rib chiqamiz:

$k=1, b[1]=1$  – boshlang'ich qiymatlar.

1-qadam.  $1 < (1+2)$  (rost)

$$k=k+3=1+3=4,$$

$$b[4]=b[1]+2=1+2=3.$$

$S[b[k]]=S[b[4]]=S[3]='F'$  ni ekranga chiqaradi.

2-qadam.  $4 < (3+2)$  (rost)

$$k=k+3=4+3=7,$$

$$b[7]=b[1]+2=3+2=5.$$

$S[b[k]]=S[b[7]]=S[5]='R'$  ni ekranga chiqaradi.

3-qadam.  $7 < (5+2)$  (yolg'on) – siki tugaydi va dastur bajarilishi to'xtaydi.

Javob: FR.

**35. Qarang: 5-variant 31-savol (43-bet).**

**36. Qarang: 21-variant 32-savol (155-bet).**