

HARBIY 5.07.2019

**MATEMATIKA YECHIMLARI
TELEGRAMDAGI MANZILIMIZ
@AXBOROTNOMA
PDF. Fariatiga o'tkazgan shahs.**

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@AXBOROTNOMA|

1. 12345...110111

$1 \cdot 9 + 2 \cdot 90 + 3 \cdot 12 = 225$ (D)

2. 12345...110111112

$1 \cdot 9 + 2 \cdot 90 + 3 \cdot 13 = 228$ (D)

3. 12345...110111

TURLI RAQAM 10 TA (B)

4. 0; 1; 2; 3; 4

$4 \cdot 5 \cdot 5 = 100$ (A)

5. 1; 2; 3; 4; 5

$5 \cdot 5 \cdot 5 = 125$ (B)

6. 0; 1; 2; 3; 4; 5; 6

$6 \cdot 7 \cdot 7 = 294$ (E) :-)

7. $2^4 = 16$ (A)

8. $2^5 = 32$ (C)

9. $A = \{a; b; c; d; e; f\}$

$n=6$ $2^6 = 64$ $2^5 = 32$ (C)
 $64 - 32 = 32$

d element qatnashmagun
qism toplamlar soni 32 ta,
qatnashgani ham 32 ta.

10. $A = \{a; b; c; d; e; f\}$

$B = \{a; b; d; e; f\}$ $C = \{a; d; e; f\}$

$n=5$ $2^5 = 32$ $n=4$ $2^4 = 16$

$32 - 16 = 16$ (A)

11. $A = \{a; b; c; d; e; f\}$

$B = \{a; b; e; f\}$

$n=4$ $2^4 = 16$ (A)

12. $A = \{a; b; c; d\}$ $C_0^4 + C_1^4 + C_2^4 = 4$

$\{a\} \{b\} \{c\} \{d\} \{a; b\} \{b; d\} \{a; b; c; d\}$

$\{a; c\} \{c; d\} \{a; b; c\} \{a; d\} \{a; b; d\}$

$\{a; b; d\} \{a; c; d\} \{b; c; d\} \{b; c\}$

13. $A = \{0; 1; 2; 5; 6; 7; 9\}$ $B = \{1; 4; 8; 9\}$

$A \cup B = \{0; 1; 2; 4; 5; 6; 7; 8; 9\}$ $n=9$

$2^9 - 2 = 512 - 2 = 510$

14. $A = \{x | x = 2n; n \in \mathbb{N}\}$

$B = \{x | x = 2n+1; n \in \mathbb{N}\}$

$A \cup B = \mathbb{N} \setminus \{1\}$ (C)

15. $A = \{x | x = 2n; n \in \mathbb{N}\}$

$B = \{x | x = 2n+1; n \in \mathbb{N}\}$

$A \cap B = \emptyset$ (D)

16. $N(2) = 63 = \left[\frac{126}{2} \right]$

$N(7) = 18 = \left[\frac{126}{7} \right]$ $63 + 18 - 9 = 72$

$N(14) = 9 = \left[\frac{126}{14} \right]$ $126 - 72 = 54$ (D)

17. $N(3) = 45$

$N(5) = 27$ $45 + 27 - 9 = 63$

$N(15) = 9$ $135 - 63 = 72$ (B)

18. $N(5) = 40 = \left[\frac{100}{5} \right]$

$N(7) = 28 = \left[\frac{100}{7} \right]$ $40 + 28 - 5 = 63$

$N(35) = 5 = \left[\frac{100}{35} \right]$ $100 - 63 = 37$ (A)

19. 324; 255; 71

(C) $E_{\text{KUB}}(324-255; 255-71) = 23$

20. $128^{143} = 128^3 = \dots 2$ (B)

21. $433^{333} = 433^1 = \dots 3$ (C)

22. $233^{233} = 233^1 = \dots 3$ (C)

23. $373^{373} = 373^1 = \dots 1$ (C)

24. $999^{999} = 999^2 = \dots 1$ (A)

25. $888^{888} = 888^4 = \dots 6$ (C)

26. $x = 44$

$x + 2 \cdot n = 62$ $n = 9$ (A)

27. $x = 52$

$x + 2 \cdot n = 72$ $n = 10$ (B)

28. $\begin{cases} x+y=1,5(x-y) & 2x+2y=3x-3y \\ x^2+y^2=254 & x^2=26 \end{cases}$ $54 = x$

$\frac{x^2+y^2}{x^2} = \frac{254}{26} = \frac{98}{10} = 9,8$ (A) 430%

$$29. a^2 - b^2 = 49.$$

$$(a+b)(a-b) = 49 \cdot 1.$$

$$\begin{cases} a+b=49 & a=25 \\ a-b=1 & b=24 \end{cases}$$

$$B) 3 \cdot 25 - 2 \cdot 24 = 75 - 48 = 27$$

$$30. a^2 - b^2 = 25.$$

$$(a+b)(a-b) = 25 \cdot 1$$

$$\begin{cases} a+b=25 & a=13 \\ a-b=1 & b=12 \end{cases} \quad C)$$

$$2 \cdot 13 - 12 = 26 - 12 = 14$$

$$31. a^2 - b^2 = 9.$$

$$(a+b)(a-b) = 9 \cdot 1$$

$$\begin{cases} a+b=9 & a=5 \\ a-b=1 & b=4 \end{cases} \quad C)$$

$$2 \cdot 5 - 3 \cdot 4 = 10 - 12 = -2.$$

$$32. (n-m)(n+m) = 25.$$

$$\begin{cases} n-m=1 & n=13 \\ n+m=25 & m=12 \end{cases} \quad B)$$

$$n+2m = 13 + 2 \cdot 12 = 37.$$

$$33. NBS(EKUB(911; 659; 647+367))$$

$$NBS(1) = 1. \quad A)$$

$$\begin{array}{r|l} 911 & 911 \\ \hline 1 & 1 \end{array} \quad \begin{array}{r|l} 659 & 659 \\ \hline 1 & 1 \end{array} \quad \begin{array}{r|l} 1014 & 2 \\ \hline 507 & 3 \\ 169 & 13 \\ 13 & 13 \\ 1 & 1 \end{array}$$

$$EKUB = 1.$$

$$34. EKUK(NBS(144); 51) = EKUK(15; 51)$$

$$144 = 2^4 \cdot 3^2 \quad NBS = (4+1)(2+1) = 15. \quad B)$$

$$\begin{array}{r|l} 15 & 3 \\ \hline 5 & 5 \\ 1 & 1 \end{array} \quad \begin{array}{r|l} 51 & 3 \\ \hline 17 & 17 \\ 1 & 1 \end{array} \quad EKUK = 3 \cdot 5 \cdot 17 = 255$$

$$35. 3a - (5a - (3a - (2a + b))) = \quad B)$$

$$\begin{aligned} &= 3a - (5a - (3a - 2a - b)) = \\ &= 3a - (5a - a + b) = 3a - 4a - b = -a - b \end{aligned}$$

$$36. 5a - (4a - (3a - (2a + b))) = \quad A)$$

$$\begin{aligned} &= 5a - (4a - (3a - 2a - b)) = \\ &= 5a - (4a - a - b) = 5a - 3a + b = 2a + b. \end{aligned}$$

$$37. \frac{1}{a(a-b)(a-c)} + \frac{1}{b(b-a)(b-c)} + \frac{1}{c(c-a)(c-b)} = X$$

$$\begin{aligned} &= \frac{1}{a(b-c)(a-c)} - \frac{1}{b(b-c)(a-b)} + \frac{1}{c(a-c)(b-c)} = \\ &= \frac{bc(b-c) - ac(a-c) + ab(a-b)}{abc(a-b)(a-c)(b-c)} = \\ &= \frac{b^2c - bc^2 - a^2c + ac^2 + a^2b - ab^2}{abc(a-b)(a-c)(b-c)} = \\ &= \frac{b^2c - bc^2 - a^2c + ac^2 + a^2b - ab^2}{abc(b^2c - bc^2 - a^2c + ac^2 + a^2b - ab^2)} = \frac{1}{abc} \quad C) \end{aligned}$$

$$38. -\frac{1}{abc} \quad 37 \text{ ni minusligi.} \quad B)$$

$$39. \frac{a+b}{a^{\frac{2}{3}} - a^{\frac{1}{3}}b^{\frac{1}{3}} + b^{\frac{2}{3}}} - \frac{a-b}{a^{\frac{2}{3}} + a^{\frac{1}{3}}b^{\frac{1}{3}} + b^{\frac{2}{3}}} = \quad A)$$

$$= a^{\frac{1}{3}} + b^{\frac{1}{3}} - a^{\frac{1}{3}} + b^{\frac{1}{3}} = 2b^{\frac{1}{3}} = 2\sqrt[3]{b}.$$

$$40. \frac{(\sqrt{a}-\sqrt{b})^3 + 2a^2\sqrt{a} + b\sqrt{b}}{a\sqrt{a} + b\sqrt{b}} + \frac{3\sqrt{ab} - 3b}{a-b}$$

$$1) \frac{\sqrt{a}^3 - 3a\sqrt{b} + 3\sqrt{a} \cdot b + b\sqrt{b} + 2a\sqrt{a} + b\sqrt{b}}{\sqrt{a}^3 + \sqrt{b}^3}$$

$$= \frac{3(a\sqrt{a} - a\sqrt{b} + \sqrt{a} \cdot b)}{(\sqrt{a} + \sqrt{b})(a - \sqrt{a}b + b)} = \frac{3\sqrt{a}}{\sqrt{a} + \sqrt{b}}$$

$$2) \frac{3\sqrt{a}}{\sqrt{a} + \sqrt{b}} + \frac{3\sqrt{ab} - 3b}{a-b} = \frac{3\sqrt{a}(\sqrt{a} - \sqrt{b}) + 3\sqrt{ab} - 3b}{a-b}$$

$$= \frac{3a - 3\sqrt{a}b + 3\sqrt{ab} - 3b}{a-b} = 3. \quad C)$$

$$41. \frac{(\sqrt{a} + \sqrt{b})^3 + 2a^2\sqrt{a} + b\sqrt{b}}{a\sqrt{a} + b\sqrt{b}} - \frac{3\sqrt{ab} + 3b}{a-b}$$

$$1) \frac{\sqrt{a}^3 + 3a\sqrt{b} + 3\sqrt{a} \cdot b + b\sqrt{b} + 2a\sqrt{a} + b\sqrt{b}}{a\sqrt{a} + b\sqrt{b}}$$

$$= \frac{3\sqrt{a}^3 + 3a\sqrt{b} + 3\sqrt{a} \cdot b}{(\sqrt{a} + \sqrt{b})(a + \sqrt{a}b + b)} = \frac{3\sqrt{a}}{\sqrt{a} + \sqrt{b}}$$

$$2) \frac{3\sqrt{a}}{\sqrt{a} + \sqrt{b}} - \frac{3\sqrt{ab} + 3b}{a-b} = \frac{3\sqrt{a}(\sqrt{a} + \sqrt{b}) - 3\sqrt{ab} - 3b}{a-b}$$

$$= \frac{3a + 3\sqrt{a}b - 3\sqrt{ab} - 3b}{a-b} = 3. \quad C)$$

42. $a=75$ $p=4$ $q=3$
 $75 \cdot 0,04 = 3$
 $75 \cdot 0,003 = 0,225$ (A)

54. $f(x) + x f\left(\frac{x}{2x-1}\right) = 2$ $f(x) = ?$
 $\frac{x}{2x-1} = a$ $x = 2ax - a$
 $a = 2ax - x$ $x = \frac{a}{2a-1}$

43. $a > 1$ (C)
 1) $\log_a \log_a \log_a 5$ 3) $\log_a \log_a \log_a 5$

(C) $\left\{ \begin{aligned} f\left(\frac{a}{2a-1}\right) + \frac{a}{2a-1} f(a) &= 2 \\ f(a) + a f\left(\frac{a}{2a-1}\right) &= 2 : a \end{aligned} \right.$

44. $0 < a < 1$ (D)
 $\log_a \log_a \log_a \frac{1}{5}$

$\frac{a}{2a-1} f(a) - \frac{1}{a} f(a) = 2 - \frac{2}{a}$ (A)

45. $y = \frac{2}{x} - 3$ $(-\infty; -3) \cup (-3; \infty)$ (B)

$\left(\frac{a}{2a-1} - \frac{1}{a}\right) f(a) = \frac{2a-2}{a}$ $f(a) = \frac{2a-2}{a} \cdot \frac{a(2a-1)}{a^2-2a+1}$

46. $y = \frac{3}{x} - 4$ $(-\infty; -4) \cup (-4; \infty)$ (B)

$f(a) = \frac{2(2a-1)}{a-1}$ $f(x) = \frac{4x-2}{x-1}$

47. $y = \frac{4}{x} - 2$ $(-\infty; -2) \cup (-2; \infty)$ (B)

55. $y = \frac{x^2}{\sqrt{x^2+5}}$ $y' = \frac{2x\sqrt{x^2+5} - x^2 \cdot \frac{2x}{2\sqrt{x^2+5}}}{x^2+5}$

48. $y = \arccos 2^x$
 $-1 \leq 2^x \leq 1$ $x \leq 0$ (C)

$= \frac{2x(x^2+5) - x^3}{(x^2+5)\sqrt{x^2+5}} = \frac{x^3+10x}{\sqrt{(x^2+5)^3}}$ (D)

49. $y = \arcsin 3^x$
 $-1 \leq 3^x \leq 1$ $x \leq 0$ (C)

56. $f(x) = x^3 - 3x^2 + 2x - 1$ $f'(2) = ?$
 $f'(x) = 3x^2 - 6x + 2$ $f'(2) = 12 - 12 + 2$
 $f'(2) = 2$ (C)

50. $f(x) = \frac{5}{x} - \sqrt{\frac{x-2}{x(x+3)}}$
 $\left\{ \begin{aligned} x \neq 0 \\ \frac{x-2}{x(x+3)} \geq 0 \end{aligned} \right.$ (B)

57. $f(x) = \frac{x^3-8}{x^2+2x+4} = x-2$

51. $f(x)$ $y = 2f(x-1) - 7$
 $(-\infty; \infty)$ (A)

$f(2x-1) = 2x-1-2 = 2x-3$
 $f'(2x-1) = 2$ (C)

52. $f(x)$ $y = 2f(x-1) - 7$
 monoton (A)

58. $f(x) = \frac{x^3-8}{x^2+2x+4} - 2x+1 = x-2-2x+1 = -x-1$
 $f'(x) = -1$ (D)

53. $\left\{ \begin{aligned} f(x) + 2f\left(\frac{1}{x}\right) &= x \\ f\left(\frac{1}{x}\right) + 2f(x) &= \frac{1}{x} \end{aligned} \right.$ (x2)

59. $f(x) = \frac{x^3-8}{x^2-2x+4}$ $f'(x) = \frac{3x^2(x^2-2x+4) - (x^3-8)(2x-2)}{(x^2-2x+4)^2}$
 $f'(0) = \frac{-16}{16} = -1$ (D)

(C) $\left\{ \begin{aligned} f(x) + 2f\left(\frac{1}{x}\right) &= x \\ 2f\left(\frac{1}{x}\right) + 4f(x) &= \frac{2}{x} \end{aligned} \right.$ (B)
 $3f(x) = \frac{2}{x} - x$ $f(x) = \frac{2-x^2}{3x}$

59. $f(x) = \frac{x^3 - 8}{x^2 + 2x + 4} - 2x + 1$

$f(x) = x - 2 - 2x + 1$

$f(x) = -x - 1$

$f'(x) = -1$ (D)

60. $y = \frac{x^3 - 27}{x^2 - 3x + 9} + 3x$ $y'(1) = ?$

$y' = \frac{3x^2(x^2 - 3x + 9) - (x^3 - 27)(2x - 3)}{(x^2 - 3x + 9)^2} + 3$

$y'(1) = \frac{3(1 - 3 + 9) - (1 - 27)(2 - 3)}{(1 - 3 + 9)^2} + 3 =$

$= \frac{21 - 26}{49} + 3 = 2 \frac{49}{49}$ (D)

61. $F'(x) = x - 4$ $F(2) = 0$. $F(x) = ?$

$F(x) = \frac{x^2}{2} - 4x + C$

$0 = 2 - 8 + C$ $C = 6$

$F(x) = \frac{x^2}{2} - 4x + 6$ (B)

62. $f(x) = 2x^2 - x$ $x = 4$ $\Delta x = 0,1$

$\Delta y = f(x + \Delta x) - f(x) = 1,52$ (C)

$f(4,1) = 2 \cdot 4,1^2 - 4,1 = 29,52$

$f(4) = 2 \cdot 4^2 - 4 = 28$

63. $f(x) = x^2 - 2x$ $x = 3$ $\Delta x = 0,1$

$\Delta y = f(x + \Delta x) - f(x) = 0,41$

$f(3,1) = 3,1^2 - 2 \cdot 3,1 = 3,41$ (B)

$f(3) = 3^2 - 2 \cdot 3 = 3$

65. $f(x) \cdot f'(x) \geq 0$

1. + - $(-\infty; -6]$

2. - - $[-6; -4]$

3. - + $[-4; -3]$ (B)

4. + + $[-3; 0]$

5. + - $[0; 4]$

6. - - $[4; 5]$

7. - + $[5; 6]$

8. + + $[6; \infty)$

64. $f(x) = -x^2 + 2x$ $x = -2$ $\Delta x = 0,1$

$\Delta y = f(x + \Delta x) - f(x)$

$\Delta y = f(-1,9) - f(-2) = -7,41 + 8 = 0,59$ (D)

$f(-1,9) = -1,9^2 + 2 \cdot 1,9 = -7,41$ $f(-2) = -4 - 4 = 8$

66. $f(x) \cdot f'(x) < 0$

1. + - $(-\infty; -6)$

2. - - $(-6; -4)$

3. - + $(-4; -3)$

4. + + $(-3; 0)$

5. + - $(0; 4)$

6. - - $(4; 5)$

7. - + $(5; 6)$ (C)

8. + + $(6; \infty)$

67. $\frac{f'(x)}{f(x)} > 0$ 65-misol ozi faqat qd' tiy. (D)

68. $0,25y' = y$ $\frac{dy}{dx} = 4y$ $\int \frac{dy}{y} = \int 4 dx$

$\ln y = 4x + C$ $y = e^{4x}$ (A)

69. $0,5y' = y$ $\frac{dy}{dx} = 2y$ $\int \frac{dy}{y} = \int 2 dx$

$\ln y = 2x + C$ $y = e^{2x}$ (A)

70. $s(t) = 2t^3 + 9t + 3$

$s'(t) = 6t^2 + 9$ (D)

71. $s(t) = -2t^3 + 9t + 15$

$s'(t) = -6t^2 + 9$ (D)

72. $y = 9 - x^2$ $x = -3$ $y = 9 - 9 = 0$

$k = -2x = 6$

$y = 6(x + 3) = 6x + 18$ (B)

73. $\int (x^3 - \cos 4x) dx = \frac{x^4}{4} - \frac{1}{4} \sin 4x + C$ (B)

74. $\int x^2 \sin x^3 dx = \int \frac{1}{3} \sin x^3 dx^3 = -\frac{1}{3} \cos x^3 + C$ (B)

75. $\int x^3 \sin x^4 dx = \int \frac{1}{4} \sin x^4 dx^4 = -\frac{1}{4} \cos x^4 + C$ (B)

76. $\int x^3 \cos x^4 dx = \int \frac{1}{4} \cos x^4 dx^4 = \frac{1}{4} \sin x^4 + C$ (C)

77. $\int \arcsin x dx$

$$77. \int \arcsin x \, dx = \left[\begin{array}{l} \arcsin x = t, \, dx = \cos t \, dt \\ x = \sin t \end{array} \right]$$

$$\int t \cdot \cos t \, dt = \left[\begin{array}{l} t = u, \, \cos t \, dt = d\sigma \\ dt = du, \, \sin t = \sigma \end{array} \right] =$$

$$= u \cdot \sigma - \int \sigma \, du = t \cdot \sin t - \int \sin t \, dt = \textcircled{B}$$

$$= t \cdot \sin t + \cos t = x \cdot \arcsin x + \sqrt{1-x^2} + C.$$

$$78. \int x \cdot a^x \, dx = \left[\begin{array}{l} x = u, \, a^x \, dx = d\sigma \\ dx = du, \, \frac{a^x}{\ln a} = \sigma \end{array} \right] =$$

$$= x \cdot \frac{a^x}{\ln a} - \int \frac{a^x}{\ln a} \, du = x \cdot \frac{a^x}{\ln a} - \frac{a^x}{\ln^2 a} + C. \textcircled{A}$$

$$79. \int x \cdot 3^x \, dx = x \cdot \frac{3^x}{\ln 3} - \frac{3^x}{\ln^2 3} + C. \textcircled{A}$$

$$80. \int \cos x \cdot e^x \, dx = \left[\begin{array}{l} \cos x = u, \, e^x \, dx = d\sigma \\ -\sin x \, dx = du, \, e^x = \sigma \end{array} \right]$$

$$= e^x \cdot \cos x + \int e^x \cdot \sin x \, dx = e^x \cdot \cos x + e^x \cdot \sin x - \int e^x \cdot \cos x \, dx$$

$$\int 2e^x \cos x \, dx = e^x \cos x + e^x \sin x.$$

$$\int e^x \cos x \, dx = \frac{e^x}{2} (\cos x + \sin x) + C \textcircled{A}$$

$$81. \int \ln(\sin x)^{\cos x} \, dx = \int \cos x \ln \sin x \, dx =$$

$$\int \ln \sin x \, d(\sin x) = \left[\sin x = t \right] = \int \ln t \, dt =$$

$$= \left[\begin{array}{l} \ln t = u \\ \frac{1}{t} \, dt = du, \, t = \sigma \end{array} \right] dt = d\sigma = t \cdot \ln t - \int t \cdot \frac{1}{t} \, dt =$$

$$= t \cdot \ln t - t + C = \sin x \cdot \ln \sin x - \sin x + C \textcircled{C}$$

$$82. \int_{-1}^1 (t^k + \sin x) \, dx = 0. \int_{-1}^1 \text{Toq funksiyalar} \, dx = 0.$$

\textcircled{B}

96. $\sin x \cdot \cos x = -0,345$. $1,6 < x < 2,1$.
 II chorak $\sin x > 0$ $\cos x < 0$.

$\sin x - \cos x = \sqrt{1 - \sin^2 x} = \textcircled{A}$
 $= \sqrt{1 + 2 \cdot 0,345} = \sqrt{1 + 0,69} = 1,3$

97. $\cos x = -\sqrt{0,2}$ $\sin(\frac{5\pi}{2} - 2x) = \textcircled{B}$
 $= \cos 2x = 2\cos^2 x - 1 = 2 \cdot 0,2 - 1 = -0,6$

98. $\frac{1 + \sin 2x}{\sin x + \cos x} - \frac{1 - \tan^2 x}{1 + \tan^2 x} = \sin x + \cos x - \cos x$
 $\sin x = \textcircled{C}$

99. $\sin 2\alpha \cos^3 \alpha + \cos 2\alpha \sin^3 \alpha = \sin 2\alpha \cos \alpha (\sin^2 \alpha + \cos^2 \alpha) =$
 $= \frac{1}{2} \sin 2\alpha = \textcircled{B}$

100. $\sin 3\alpha \cos^3 \alpha + \cos 3\alpha \sin^3 \alpha =$
 $= (3\sin \alpha - 4\sin^3 \alpha) \cos^3 \alpha + (4\cos^3 \alpha - 3\cos \alpha) \sin^3 \alpha =$
 $= 3\sin \alpha \cos^3 \alpha - 4\sin^3 \alpha \cos^3 \alpha + 4\cos^3 \alpha \sin^3 \alpha - 3\cos \alpha \sin^3 \alpha =$
 $= 3\sin \alpha \cos \alpha (\cos^2 \alpha - \sin^2 \alpha) = \frac{3}{2} \sin 2\alpha \cos 2\alpha =$
 $= \frac{3}{4} \sin 4\alpha = \textcircled{C}$

101. $\frac{\sin(2y+x) + \sin(2y-x)}{\sin x - \sin(2y-x)} \cdot \frac{\tan y - \tan x}{\tan y} =$
 $= \frac{2 \sin y \cos x}{2 \cos y \sin(x-y)} \cdot \frac{\sin(y-x)}{\sin y \cos x \cos y} =$
 $= \frac{2 \sin y \cos y}{\cos y \cdot \frac{\sin y}{\cos y} \cdot \cos y} = -2 = \textcircled{A}$

102. $\frac{\sin(2x+y) + \sin(2x-y)}{\sin(x+y) + \sin y} \cdot \frac{\tan y + \tan x}{\tan x} = \textcircled{C}$
 $= \frac{2 \sin 2x \cos y}{2 \sin(x+y) \cos x} \cdot \frac{\sin(x+y)}{\cos x \cos y \cdot \tan x} = 2$

103. $\frac{\sin(4x+y) + \sin(4x-y)}{\sin y - \sin(4x-y)} \cdot \frac{\tan y - \tan 2x}{\tan 2x} =$
 $\textcircled{A} = \frac{2 \sin 4x \cdot \cos y}{2 \cos 2x \cdot \sin(2x-y)} \cdot \frac{\sin(2x-y)}{(\sqrt{3}-4)(\sqrt{\sqrt{3}-3}-1)} = -2$

104. $\frac{\sqrt{3}-4}{\sqrt{\sqrt{3}-3}+1} - \frac{\sqrt{\sqrt{3}-12}}{\sqrt{\sqrt{3}-3}-3} = \frac{(\sqrt{3}-4)(\sqrt{\sqrt{3}-3}+3)}{\sqrt{3}-3-1} =$
 $= \frac{(\sqrt{3}-4)(\sqrt{\sqrt{3}-3}+3)}{\sqrt{3}-4} = \sqrt{\sqrt{3}-3}-1 + \sqrt{\sqrt{3}-3}+3 =$
 $= 2 = \textcircled{D}$

105. $\frac{\sqrt{21}-4}{\sqrt{\sqrt{21}-3}-1} - \frac{\sqrt{21}-12}{\sqrt{\sqrt{21}-3}+3} =$
 $= \frac{(\sqrt{21}-4)(\sqrt{\sqrt{21}-3}+1)}{\sqrt{21}-3-1} - \frac{(\sqrt{21}-12)(\sqrt{\sqrt{21}-3}-3)}{\sqrt{21}-3-9} =$
 $= \sqrt{\sqrt{21}-3}+1 - \sqrt{\sqrt{21}-3}-3 = -2 = \textcircled{C}$

106. $\frac{\sqrt{23}-4}{\sqrt{\sqrt{23}-3}-1} - \frac{\sqrt{23}-12}{\sqrt{\sqrt{23}-3}+3} =$
 $= \frac{(\sqrt{23}-4)(\sqrt{\sqrt{23}-3}+1)}{\sqrt{23}-3-1} - \frac{(\sqrt{23}-12)}{\sqrt{23}-12} =$
 $= \frac{(\sqrt{23}-3)-3}{\sqrt{23}-3-1} =$
 $= \frac{\sqrt{23}-6}{\sqrt{23}-4} = \sqrt{\sqrt{23}-3}+1 - \sqrt{\sqrt{23}-3}+3 =$
 $= 4 = \textcircled{B}$

107. $\frac{\sqrt[3]{(5+2\sqrt{6})^2}}{\sqrt[3]{5-\sqrt{24}}} - 6 - \sqrt{24} =$
 $\textcircled{B} = \sqrt[3]{\frac{(5+2\sqrt{6})^3}{25-24}} - 6 - \sqrt{24} = -1$

108. $16 \sin 10^\circ \cdot \sin 20^\circ \cdot \sin 50^\circ =$
 $\textcircled{A} \sin 70^\circ \cdot \sin 90^\circ =$
 $= 16 \cdot \frac{1}{4} \sin 30^\circ \cdot \sin 30^\circ = 4 \cdot \frac{1}{2} \cdot \frac{1}{2} = 1$

109. $32 \cos 10^\circ \cdot \cos 30^\circ \cdot \cos 50^\circ =$
 $\cos 60^\circ \cdot \cos 70^\circ =$
 $\frac{32}{2} \cdot \frac{\sqrt{3}}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cos 30^\circ =$
 $= 2\sqrt{3} \cdot \frac{\sqrt{3}}{2} = 3 = \textcircled{B}$

110. $\lg \tan 1^\circ + \lg \tan 2^\circ + \dots + \lg \tan 89^\circ =$
 $= \lg \tan 1^\circ \cdot \tan 2^\circ \cdot \dots \cdot \tan 89^\circ = 0 = \textcircled{C}$
 $\tan x \cdot \tan y = 1, x+y=90^\circ$

111. $\lg \tan 1^\circ \cdot \lg \tan 2^\circ \cdot \dots \cdot \lg \tan 89^\circ =$
 $\lg \tan 45^\circ = \lg 1 = 0 = \textcircled{C}$

112. $\lg \sin 1^\circ \cdot \lg \sin 2^\circ \cdot \lg \sin 3^\circ \dots \lg \sin 90^\circ =$
 (B) $= 0$. $\lg \sin 90^\circ = \lg 1 = 0$.

113. $2^{|x+2|} > 16$ $|x+2| > 4$.
 $x+2 > 4$ $x > 2$
 $x+2 < -4$ $x < -6$ (A)

114. $x^4 \cdot 2^x + 8 > 8x^4 + 2^x$
 $x^4(2^x - 8) - (2^x - 8) > 0$
 $(2^x - 8)(x^4 - 1) > 0$
 $x = 3$ $x = \pm 1$ (A)

115. $(0, 3)^{2+4+6+\dots+2x} > (0, 3)^{72}$
 $2+4+6+\dots+2x < 72$
 $\frac{2+2x}{2} \cdot x < 72$ $x^2 + x - 72 < 0$
 $(-9, 8)$

116. $\arccos x < \arcsin x$
 $\frac{\pi}{2} - \arcsin x < \arcsin x$
 $\arcsin x > \frac{\pi}{4}$
 $(\frac{\sqrt{2}}{2}, 1]$ (B)

117. $\arctan x \geq \arccot x$
 $\arctan x \geq \frac{\pi}{2} - \arctan x$
 $2\arctan x \geq \frac{\pi}{2}$ $\arctan x \geq \frac{\pi}{4}$
 $[1, \infty)$ (A)

118. $\frac{(\sqrt{3x-7})^2 - 2}{x-3} \leq \frac{3 - (\sqrt{x})^2}{x-3}$
 $\begin{cases} 3x-7 > 0, x \geq \frac{7}{3} \\ x > 0 \end{cases}$
 $\frac{3x-7-2}{x-3} \leq \frac{3-x}{x-3}$
 $\frac{3x-9}{x-3} \leq -1$
 $3 \leq -1$ \emptyset

119. $\frac{36-x^2}{6x^2-x} \geq 0$ $\frac{(6-x)(6+x)}{(6-x)x^2} \geq 0$
 $\begin{cases} x^2(6+x) \geq 0 \\ 6-x \neq 0 \end{cases}$

(B) $\frac{5+7+8+9+10+11+12}{7} = \frac{5+12}{2} = 8\frac{1}{2}$ $[5, 13]$

120. $\frac{x^2-49}{-7x^2+x} \leq 0$ $\frac{x^2-49}{x-7} \leq 0$
 $\begin{cases} (x+7)x^2 \leq 0 \\ x-7 \neq 0 \end{cases}$

(C) $\frac{-9-8-7}{3} = -8$ $[-9, 1]$

120. $\frac{64-x^2}{8x^2-x} \geq 0$ $[5, 13]$

$\frac{(8-x)(8+x)}{8-x} \geq 0$
 $\frac{x^2}{x^2} \geq 0$
 $\begin{cases} x^2(8+x) \geq 0 \\ 8-x \neq 0 \end{cases}$

$\frac{5+6+7+9+10+11+12}{7} = \frac{5+12}{2} = 8\frac{1}{2}$

122. $\frac{x^2-121}{-11x^2+x} \geq 0$ $(3, 12)$

$\frac{(x-11)(x+11)}{x-11} \geq 0$ $\begin{cases} x^2(x+11) \geq 0 \\ x-11 \neq 0 \end{cases}$

$\frac{4+10}{2} = 7$ (B)

123. $\log_{18}(3x+1) > \frac{1}{2}$
 $3x+1 > 3\sqrt{2}$
 $x > \frac{3\sqrt{2}-1}{3}$ (A)